# Molecular Connectivity VII: Specific Treatment of Heteroatoms 

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#### Abstract

The molecular connectivity index, $\chi$, initially designed for hydrocarbons, has been formally extended to molecules containing heteroatoms. The $\delta$ value of the heteroatom is modified to take account of its number of attached hydrogen atoms, $\delta_{i}{ }^{v}=Z^{v}-h_{i}$. These values were successfully tested on boiling points and molar refractions. A table of $\delta^{U}$ values is presented for nitrogen, oxygen, fluorine, chlorine, bromine, and iodine in various bonding situations.

Keyphrases Molecular connectivity-heteroatomic molecules, correlated with boiling points and molar refractions $\square$ Heteroatomic molecules-molecular connectivity indexes calculated, correlated with boiling points and molar refractions $\square$ Boiling points-heteroatomic molecules, correlated with molecular connectivity indexes a Molar refractions-heteroatomic molecules, correlated with molecular connectivity indexes


In earlier studies using the molecular connectivity index, $\chi$, to describe structural features, the heteroatoms oxygen and nitrogen were considered to contribute equally with carbon (1-7). This designation inevitably led to redundant values of $\chi$ for isomers such as 2-methyl-1-propanol and 2-methyl-2-propanol. An initial approach to the resolution of these redundancies was used in an alcohol solubility study (2). A second regression variable was introduced simply as the contribution to total $\chi$ from the $\mathrm{C}-\mathrm{OH}$ bond. This bond value varies in primary, secondary, and tertiary alcohols. Redundancies are destroyed, and there is a $16 \%$ decrease in the standard error for the $\log$ of the solubility. A $33 \%$ decrease in the boiling-point standard error is also observed for this empirical approach.
In a second empirical approach, the total degree of branching, $\Delta x$, in the heteroatom-containing molecule is partitioned. The branching attributed to functional group position, $\Delta \chi^{F}$, is separated from that due to carbon skeleton branching, $\Delta \chi^{S}$. In a study of the heat of atomization of 20 saturated noncyclic alcohols, the standard error was reduced $40 \%$ when these quantities were introduced into the regression (3).

These approaches are now considered to be an interim or first-order solution to a more basic problem of calculating the molecular connectivity contribution of any atom other than carbon.

## METHOD

An alternative approach to heteroatom calculation has a basis in earlier considerations of unsaturated molecules (4). That study used the valence connectedness of the atom as a $\delta$ value for carbon atoms in a double bond. Thus, the central carbon of propene has a $\delta$ of 3 , the central carbon of 2-methylpropene has a $\delta$ of 4, and both carbons of ethene have a $\delta$ of 2 . Use of these values gives rise to a $\chi$ for the molecule designated as a valence $\chi$ or $\chi^{v}$. Benzene would thus have a $\chi^{v}$ of 2.000 [not modifying for the cyclic nature of the molecule (1)].

There are several ways that this $\delta$ value can be understood within the framework of the connectivity theory already developed (1-7). It can be derived from the total number of bonds emanating from the atom, counting the $\pi$ electron bonds as well as the $\sigma$ bonds.

Another derivation for the $\delta$ value is its equivalence to the number of valence electrons, $Z^{v}$, minus the number of hydrogen atoms, $h$, bonded to the atom under consideration, $Z^{\prime \prime}-h$.

Table I—Valence Delta ( $\delta^{v}$ ) Values for Heteroatoms

| Group | $\delta^{v}$ | Group | $\delta^{v}$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{NH}_{2}$ | 3 | OH | 5 |
| NH | 4 | O | 6 |
| N | 5 | $\mathrm{C}=\mathrm{O}$ | 6 |
| $\mathrm{C}=\mathrm{N}$ | 5 | Furan O | 6 |
| $\mathrm{C}=\mathrm{NH}$ | 4 | $\mathrm{O}=\mathrm{NO}$ | 6 |
| Pyridine N | 5 | $\mathrm{H}_{2} \mathrm{O}$ | 4 |
| Nitro N | 6 | $\mathrm{H}_{3} \mathrm{O}^{+}$ | 3 |
| $\mathrm{NH}^{3}+$ | 2 | F | $(-) 20$ |
| $\mathrm{NH}_{4}{ }^{+}$ | 1 | Cl | 0.690 |
| $>\mathrm{N}^{+}$ | 6 | Br | 0.254 |
| $=\mathrm{NH}_{2}{ }^{+}$ | 3 | I | 0.085 |

Both derivations give identical values for simple unsaturated systems, but the second derivation has more wide ranging applications, especially as an approach to parameterizing the connectivity of heteroatoms.

Using the expression $\delta^{v}=Z^{v}-h$, the valence $\delta^{v}$ values for oxygen and nitrogen in several variations of bonding can be calculated (Table 1). Ammonia and water are unique limiting cases of the $Z^{v}-h$ expression. The nitro group nitrogen has a $\delta^{\circ}=6$, since it can be considered to be derived from a nitroso group ( $\delta_{N^{v}}=5$ ) by appending another connection, namely an oxygen atom bonded to the nitrogen atom. The nitrogen atom of a tetraalkylammonium ion can, by the same argument, be assigned a $\delta^{\nu}$ of 6 .

Boiling Point and Solubility-The validity of these values can be tested by determining their ability to destroy redundant $\chi$ values in a series of molecules and to improve a correlation with a physical property. The first test of the influence of the $\chi^{v}$ term is with a series of aliphatic alcohols (Table II). When using the standard connectivity $\chi$, the regression equation and statistics for the boiling points are:

$$
\begin{gather*}
\text { boiling point }=38.79( \pm 1.61) \chi+11.26( \pm 5.85) \\
r=0.963 \quad s=8.39^{\circ} \quad n=48 \tag{Eq.1}
\end{gather*}
$$

If the $\chi^{v}$ value is introduced, the relationship improves to:
boiling point $=196.58( \pm 11.34) \chi-157.6( \pm 11.31) \chi^{v}$ $-41.24( \pm 4.56)$

$$
\begin{equation*}
r=0.993 \quad s=3.68^{\circ} \quad n=48 \tag{Eq.2}
\end{equation*}
$$

The use of the second term, $x^{v}$, leads to over a twofold improvement in the standard deviation of the mean. This equation leads to a prediction of the boiling point to within $2.5 \%$.

For this same list of alcohols, the log molar solubility is related to $\chi$ by:

$$
\begin{gather*}
\log S=-2.61( \pm 0.086) \chi+6.52( \pm 0.31) \\
r=0.976 \quad s=0.447 \quad n=48 \tag{Eq.3}
\end{gather*}
$$

When using the $\chi^{v}$ term, the multiple regression equation is:

$$
\begin{gather*}
\log S=9.27( \pm 0.98) \chi+6.64( \pm 0.97) \chi^{v}+8.73( \pm 0.39) \\
r=0.988 \quad s=0.317 \quad n=48 \tag{Eq.4}
\end{gather*}
$$

The predicted values are shown in Table II.
Again, the improvement in the relationship is noteworthy upon the introduction of the $\chi^{v}$ term. The major effect is the influence of $\chi^{"}$ in destroying the seven pairs of redundant $\chi$ values in the list. Furthermore, the $\chi^{v}$ term reorders these redundancies in the correct order relative to the boiling point and $\log$ solubility.

The value of the $\chi^{v}$ term is dramatically illustrated in the case of the boiling points of several glycols (Table III):

$$
\begin{gather*}
\text { boiling point }=20.71( \pm 24.28) \chi+159.38( \pm 67.23) \\
r=0.307 \quad s=34.0^{\circ} \quad n=9 \tag{Eq.5}
\end{gather*}
$$

and:

Table II—Boiling Points and Solubilities of Saturated Alcohols

| Compound | Boiling Point |  | Log Solubility |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Obs. ${ }^{a}$ | Calc. | Obs. ${ }^{b}$ | Calc. |
| 1-Butanol | $117.7^{\circ}$ | $114.56^{\circ}$ | 0.005 | $-0.191$ |
| 2-Methylpropanol | $107.9^{\circ}$ | $108.74^{\circ}$ | $0.022$ | $0.195$ |
| 2-Butanol | $99.5{ }^{\circ}$ | $97.40{ }^{\circ}$ | 0.065 | 0.673 |
| 1-Pentanol | $137.8^{\circ}$ | $134.27^{\circ}$ | -1.347 | 1.511 |
| 3-Methylbutanol | $131.2^{\circ}$ | $128.25^{\circ}$ | -1.167 | -1.115 |
| 2-Methylbutanol | $128.7^{\circ}$ | $129.74^{\circ}$ | -1.058 | -1.214 |
| 2-Pentanol | $119.0^{\circ}$ | $116.91^{\circ}$ | -0.634 | -0.636 |
| 3-Pentanol | $115.3^{\circ}$ | $118.39^{\circ}$ | $-0.486$ | -0.736 |
| 3-Methyl-2-butanol | $111.5^{\circ}$ | $111.76^{\circ}$ | -0.404 | -0.294 |
| 2-Methyl-2-butanol | $102.0^{\circ}$ | $102.33^{\circ}$ | 0.338 | 0.180 |
| 1-Hexanol | $157.0^{\circ}$ | $153.58^{\circ}$ | -2.790 | -2.812 |
| 2-Hexanol | $139.9^{\circ}$ | $136.42^{\circ}$ | -1.995 | -1.947 |
| 3-Hexanol | $135.4{ }^{\circ}$ | $137.90^{\circ}$ | -1.832 | -2.046 |
| 3-Methyl-3-pentanol | $122.4{ }^{\circ}$ | $124.23^{\circ}$ | -0.830 | -1.289 |
| 2-Methyl-2-pentanol | $121.4^{\circ}$ | $121.85{ }^{\circ}$ | -1.117 | -1.129 |
| 2-Methyl-3-pentanol | $126.5{ }^{\circ}$ | $132.75^{\circ}$ | -1.609 | -1.704 |
| 3-Methyl-2-pentanol | $134.2^{\circ}$ | $132.75^{\circ}$ | -1.639 | -1.704 |
| 2,3-Dimethyl-2-butanol | $118.6^{\circ}$ | $117.08^{\circ}$ | -0.850 | -0.813 |
| 3,3-Dimethyl-1-butanol | $143.0^{\circ}$ | $139.81^{\circ}$ | -2.590 | -1.887 |
| 3,3-Dimethyl-2-butanol | $120.0^{\circ}$ | $123.86^{\circ}$ | -1.410 | -1.099 |
| 4-Methyl-1-pentanol | $151.8^{\circ}$ | $147.77^{\circ}$ | -2.282 | -2.425 |
| 4-Methyl-2-pentanol | $131.7^{\circ}$ | $130.61^{\circ}$ | -1.814 | -1.560 |
| 2-Ethylbutanol | $146.5^{\circ}$ | $150.73^{\circ}$ | -2.787 | -2.624 |
| 1-Heptanol | $176.3^{\circ}$ | $173.09^{\circ}$ | -4.166 | -4.122 |
| 2-Methyl-2-hexanol | $142.5^{\circ}$ | $141.36^{\circ}$ | -2.473 | -2.440 |
| 3-Methyl-3-hexanol | $142.4^{\circ}$ | $143.74^{\circ}$ | -2.263 | -2.600 |
| 3-Ethyl-3-pentanol | $142.5{ }^{\circ}$ | $146.12^{\circ}$ | -1.917 | -2.759 |
| 2,3-Dimethyl-2-pentano | $139.7^{\circ}$ | $130.99^{\circ}$ | -2.002 | -1.924 |
| 2,3-Dimethyl-3-pentanol | $139.0^{\circ}$ | $138.97^{\circ}$ | -1.937 | -2.284 |
| 2,4-Dimethyl-2-pentanol | $133.0^{\circ}$ | $135.54{ }^{\circ}$ | $-2.145$ | -2.053 |
| 2,4-Dimethyl-3-pentanol | $138.8^{\circ}$ | $147.47^{\circ}$ | -2.800 | -2.689 |
| 2,2-Dimethyl-3-pentanol | $136.0^{\circ}$ | $144.85^{\circ}$ | -2.643 | -2.509 |
| 3-Heptanol | $156.8{ }^{\circ}$ | $157.42^{\circ}$ | -3.194 | -3.357 |
| 4-Heptanol | $155.0^{\circ}$ | $157.42^{\circ}$ | -3.196 | -3.357 |
| 1-Octanol | $195.2^{\circ}$ | $192.61^{\circ}$ | -5.401 | -5.433 |
| 2,2,3-Trimethyl-3pentanol | $152.5^{\circ}$ | $151.11^{\circ}$ | -2.931 | -3.095 |
| 2-Octanol | $179.8{ }^{\circ}$ | $175.45^{\circ}$ | -4.755 | -4.568 |
| 2-Ethylhexanol | $184.6{ }^{\circ}$ | $189.76^{\circ}$ | $-5.005$ | -5.245 |
| 1-Nonanol | $213.1^{\circ}$ | $212.12^{\circ}$ | -6.907 | -6.743 |
| 2-Nonanol | $198.5^{\circ}$ | $194.96^{\circ}$ | -6.319 | -5.878 |
| 3-Nonanol | $194.7^{\circ}$ | $196.44^{\circ}$ | -6.119 | -5.978 |
| 4-Nonanol | $193.0^{\circ}$ | $196.44^{\circ}$ | -5.952 | -5.978 |
| 5-Nonanol | $195.1^{\circ}$ | $196.44^{\circ}$ | $-5.744$ | -5.978 |
| 2,6-Dimethyl-3-heptanol | $178.0^{\circ}$ | $174.40^{\circ}$ | -5.776 | -4.785 |
| 3,5-Dimethyl-4-heptanol | $187.0^{\circ}$ | $189.45^{\circ}$ | -5.298 | -5.509 |
| 1,1-Diethylpentanol | $192.0^{\circ}$ | $185.14^{\circ}$ | -5.572 | -5.381 |
| 7-Methyloctanol | $206.0{ }^{\circ}$ | $206.30^{\circ}$ | -5.744 | -6.357 |
| 3,5,5-Trimethylhexanol | $193.0^{\circ}$ | $194.1^{\circ}$ | -5.769 | -5.531 |

a Boiling points are in degrees centigrade, and the logarithms of the solubility (expressed as molality) were taken from the following sources and references cited therein: G. L. Amidon, S. H. Yalkowski, and S. J. Leung, J. Pharm. Sci., 63, 1858(1974), and "Handbook of Chemistry and Physics," 51st ed., Chemical Rubber Co., Cleveland, Ohio, 1971.
boiling point $=249.64( \pm 10.04) \chi-222.1( \pm 9.38) \chi^{U}$
$-29.11( \pm 10.92)$

$$
r=0.995 \quad s=3.78^{\circ} \quad n=9
$$

(Eq. 6)
The use of $\chi^{v}$ with the $\chi$ term lowers the $s$ value almost 10 -fold.
The use of the $\chi^{v}$ terms in the case of primary and secondary amines (Table IV) also significantly improves the correlation of connectivity indexes with the boiling points. For a series of primary amines, the equations and statistics are:

$$
\begin{align*}
& \text { boiling point }=50.93( \pm 1.00) \chi-49.17( \pm 3.30) \\
& r=0.996 \quad s=4.59^{\circ} \quad n=21 \tag{Eq.7}
\end{align*}
$$

and:
boiling point $=154.09( \pm 17.20) \chi-103.5( \pm 17.84) \chi^{v}$
$-75.92( \pm 5.03)$

$$
\begin{equation*}
r=0.999 \quad s=2.79^{\circ} \quad n=21 \tag{Eq.8}
\end{equation*}
$$

For secondary amines, the relationships are:

Table III—Boiling Points of Polyols

|  | Boiling Point |  | Connectivity Index |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Obs. ${ }^{\text {a }}$ | Calc. | X | $\chi^{v}$ |
| 2-Methyl-2,4-pentanediol | $196.0^{\circ}$ | $197.3^{\circ}$ | 3.417 | 2.821 |
| Ethanediol | $197.8^{\circ}$ | $197.3^{\circ}$ | 1.914 | 1.132 |
| 1,3-Butanediol | $207.5^{\circ}$ | $204.8{ }^{\circ}$ | 2.770 | 2.060 |
| 1,3-Propanediol | $214.7^{\circ}$ | $211.0^{\circ}$ | 2.414 | 1.632 |
| 1,2-Propanediol | $187.4^{\circ}$ | $191.1^{\circ}$ | 2.270 | 1.560 |
| 2,3-Butanediol | $181.7^{\circ}$ | $185.6^{\circ}$ | 2.643 | 2.004 |
| 1,4-Butanediol | $230.0^{\circ}$ | $224.8{ }^{\circ}$ | 2.914 | 2.132 |
| 1,5-Pentanediol | $2388^{\circ}$ | $238.5^{\circ}$ | 3.414 | 2.632 |
| Glycerol | $290^{\circ}$ | $292.7^{\circ}$ | 2.808 | 1.707 |

$a_{\text {Boiling points were taken from the "Handbook of Tables for }}$ Organic Compound Identification," 3rd ed., CRC Press, Cleveland, Ohio, 1967.

$$
\begin{align*}
& \text { boiling point }=48.50( \pm 1.15) \chi-58.55( \pm 4.07) \\
& r=0.997 \quad s=4.28^{\circ} \quad n=13 \tag{Eq.9}
\end{align*}
$$

and:
boiling point $=171.40( \pm 21.84) \chi-120.07( \pm 21.45) \chi^{v}$
$-102.4( \pm 8.07)$

$$
r=0.999 \quad s=2.20^{\circ} \quad n=13
$$

(Eq. 10)
The primary and secondary amines must apparently be considered separately with the framework of the present development of connectivity indexes. The intermolecular forces between primary amines differ enough from intermolecular forces between secondary amines,

Table IV-Boiling Points of Primary and Secondary Aliphatic Amines

| Compound | Boiling Point |  | Residual |
| :---: | :---: | :---: | :---: |
|  | Obs. ${ }^{\text {a }}$ | Calc. |  |
| Primary Amines |  |  |  |
| $n$-Propylamine | $49.0^{\circ}$ | $51.91^{\circ}$ | -2.91 |
| 2-Aminopropane | $33.0{ }^{\circ}$ | $37.00^{\circ}$ | -4.00 |
| 2-Amino-2-methylpropane | $46.0^{\circ}$ | $47.15^{\circ}$ | -1.15 |
| 2-Aminobutane | $63.0^{\circ}$ | $64.23^{\circ}$ | -1.23 |
| 2-Methylpropylamine | $69.0{ }^{\circ}$ | $69.93{ }^{\circ}$ | -0.93 |
| $n$-Butylamine | $77.0{ }^{\circ}$ | $77.21^{\circ}$ | -0.21 |
| 2-Amino-2-methylbutane | $78.0{ }^{\circ}$ | $75.66^{\circ}$ | 2.35 |
| 2 -Aminopentane | $92.0{ }^{\circ}$ | $89.54{ }^{\circ}$ | 2.45 |
| 3-Methylbutylamine | $96.0^{\circ}$ | $95.23^{\circ}$ | 0.77 |
| 2-Methylbutylamine | $96.0{ }^{\circ}$ | $97.16^{\circ}$ | -1.16 |
| $n$-Pentylamine | $104.0^{\circ}$ | $102.52^{\circ}$ | 1.47 |
| 4-Methylpentylamine | $125.0^{\circ}$ | $120.54^{\circ}$ | 4.45 |
| $n$-Hexylamine | $130.0^{\circ}$ | $127.83^{\circ}$ | 2.17 |
| 3-Methylpentylamine | $114.0^{\circ}$ | $114.85^{\circ}$ | -0.85 |
| 4-Aminoheptane | $139.0^{\circ}$ | $142.08^{\circ}$ | -2.58 |
| 2-Aminoheptane | $142.0^{\circ}$ | $136.44^{\circ}$ | 5.56 |
| $n$-Heptylamine | $155.0^{\circ}$ | $153.14^{\circ}$ | 1.86 |
| $n$-Octylamine | $180.0^{\circ}$ | $178.45^{\circ}$ | 1.55 |
| $n$-Nonylamine | $201.0^{\circ}$ | $203.76^{\circ}$ | -2.76 |
| 2-Aminoundecane | $237.0^{\circ}$ | $241.40^{\circ}$ | -4.40 |
| 3-Aminopentane | $91.0^{\circ}$ | $91.47^{\circ}$ | -0.47 |
| Secondary Amines |  |  |  |
| $N$-(Methyl)ethylamine | $36.0^{\circ}$ | $37.19^{\circ}$ | -1.19 |
| $N$-Methyl-1-methylethylamine | $50.0^{\circ}$ | $52.09^{\circ}$ | -2.09 |
| Diethylamine | $56.0^{\circ}$ | $55.28^{\circ}$ | 0.72 |
| $N$-Methyl-1-methylpropylamine | $78.5{ }^{\circ}$ | $79.35^{\circ}$ | -0.85 |
| $N$-(Ethyl)propylamine | $80.5{ }^{\circ}$ | $80.62^{\circ}$ | -0.12 |
| Bis(1-methylethyl)amine | $84.0{ }^{\circ}$ | $84.84{ }^{\circ}$ | -0.84 |
| $N$-(Methyl)butylamine | $90.5^{\circ}$ | $87.86^{\circ}$ | 2.64 |
| $N$-Methyl-1-methylbutylamine | $105.0{ }^{\circ}$ | $104.69^{\circ}$ | 0.31 |
| Dipropylamine | $109.5^{\circ}$ | $105.95{ }^{\circ}$ | 3.55 |
| Bis(2-methylpropyl)amine | $139.0^{\circ}$ | $142.03^{\circ}$ | -3.03 |
| Dibutylamine | $159.0^{\circ}$ | $156.62{ }^{\circ}$ | 2.38 |
| Bis( 3-methylbutyl)amine | $187.5^{\circ}$ | $186.66^{\circ}$ | 0.84 |
| Dipentylamine | $205.0^{\circ}$ | $207.29^{\circ}$ | -2.29 |

[^0]Table V-Substituent Parameters for Molar Refraction ( $R_{m}$ )

| Substituent | Molar Refraction |  | Connectivity Index ${ }^{b}$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Obs. ${ }^{\text {a }}$ | Calc. | $\chi^{c}$ | $\chi^{v}$ |
| Methyl | 4.7 | 4.14 | 0.577 | 0.500 |
| Ethyl | 9.4 | 9.58 | 1.115 | 1.06 |
| Propyl | 14.0 | 14.48 | 1.615 | 1.561 |
| 1-Methylethyl | 14.0 | 13.30 | 1.488 | 1.443 |
| Butyl | 18.7 | 19.37 | 2.115 | 2.061 |
| 1,1-Dimethylethyl | 18.5 | 16.29 | 1.789 | 1.750 |
| Phenyl | 24.3 | 22.84 | 3.150 | 2.161 |
| Hydroxyl | 1.5 | 2.17 | 0.577 | 0.224 |
| Methoxyl | 6.5 | 6.37 | 1.115 | 0.612 |
| Ethoxyl | 11.3 | 11.90 | 1.615 | 1.200 |
| Propoxyl | 15.9 | 16.80 | 2.115 | 1.700 |
| 1-Methylethoxyl | 16.0 | 15.66 | 1.971 | 1.595 |
| Butoxyl | 20.7 | 21.69 | 2.615 | 2.200 |
| Pentoxyl | 25.3 | 26.59 | 3.115 | 2.700 |
| Phenoxyl | 26.6 | 25.25 | 3.633 | 2.319 |
| Acetate | 11.6 | 12.22 | 1.971 | 1.112 |
| Amino | 4.2 | 2.95 | 0.577 | 0.333 |
| Acetamido | 14.6 | 12.87 | 1.971 | 1.204 |
| Nitro | 6.0 | 6.83 | 1.488 | 0.537 |
| Aldehydo | 5.3 | 5.74 | 1.115 | 0.524 |
| Acyl | 9.9 | 9.81 | 1.488 | 0.954 |
| Methylcarboxylate | 11.4 | 12.03 | 2.026 | 1.066 |
| Ethylcarboxylate | 16.2 | 17.56 | 5.526 | 1.654 |
| Amido | 8.8 | 8.30 | 1.488 | 0.743 |
| Cyano | 5.2 | 5.85 | 1.115 | 0.539 |
| Fluoro ${ }^{\text {c }}$ | -0.4 |  | 0.577 | -0.124 |
| Chloro ${ }^{\text {c }}$ | 4.8 | - | 0.577 | 0.602 |
| Bromo ${ }^{\text {c }}$ | 7.6 | - | 0.577 | 0.992 |
| Iodo ${ }^{\text {c }}$ | 12.8 | - | 0.577 | 1.719 |

$a$ Data were taken from Ref. 8. ${ }^{b}$ Connectivity index was calculated only for the substituent as if attached to the phenyl ring. $c$ No $R_{m}$ values are shown as calculated for the halogens because the observed $R_{m}$ values were used to calculate the $\delta^{\boldsymbol{v}}$ value for the halogens.
in the bulk phase, to give rise to a different boiling point for comparable connectivity indexes. Thus, diethylamine and butylamine have similar $\chi^{v}$ values ( 2.121 and 2.115), but the boiling points differ by $21^{\circ}$. The difference is probably due to differing electron densities in the lone-pair electron orbitals and the different number of amino hydrogen atoms capable of hydrogen bonding. These effects are not encoded in the connectivity indexes at the present level of development. Therefore, it is necessary to consider classes of amines when relating boiling point with molecular connectivity indexes. This question will be discussed in a subsequent paper.

Molar Refraction-If these or similar intermolecular effects are minimal in influencing a physical property, it may be possible to relate the connectivity of various molecules, containing different heteroatoms, with that property. This approach appears to be possible with molar refraction (Table V). A comparison of $\chi$ and $\chi^{\nu}$ values with molar refraction provides a severe test of the $\chi^{v}$ values because they must recreate connectivity properties of carbon, nitrogen, and oxygen in a self-consistent manner.

Twenty-five phenyl substituent group molar refractions, listed by Norrington et al. (8), were used. This list includes alkyls, ethers, amines, esters, amides, ketones, an aldehyde, alcohol, and a nitro group. The relationship is:

$$
\begin{gather*}
R_{m}=2.656( \pm 0.593) \chi+7.140( \pm 0.688) \chi^{v}-0.958( \pm 0.518) \\
r=0.990 \quad s=1.03 \quad n=25 \tag{Eq.11}
\end{gather*}
$$

This successful relationship illustrates the consistency of the oxygen and nitrogen connectivity parameters with the parameters established for the carbon atom. All $\chi$ and $\chi^{v}$ parameters are derived nonempirically from basic considerations of connectivity defined in terms of simple branching and the number of valence electrons not bonding to a hydrogen atom.

With these parameters, we have increased the ability of connectivity indexes to correlate with certain properties such as the boiling point within classes of molecular types. Furthermore, with other properties like molar refraction, these heteroatom parameters permit the correlation of connectivity indexes among mixed molecular types.

Table V includes a number of halogen-containing molecules. It would be highly desirable if these atoms could be considered within the framework of molecular connectivity. A derivation of $\delta^{\nu}$ values based upon the $\delta^{v}=Z^{v}-h$ relationship is not satisfactory. The values would obviously be 7 for each halogen. At this time, it is necessary to develop empirical parameters for the halogens, fitting them to molar refraction data such as those in Table V. These empirical $\delta^{\nu}$ values for halogens are listed in Table I.

A test of the $\delta^{v}$ values for the halogens to determine their internal consistency can be made by considering the ability of $\chi$ and $\chi^{v}$ to predict the boiling points of a mixed list of alkyl halides (Table VI). This objective is accomplished quite satisfactorily from the equation:

$$
\begin{aligned}
& \text { boiling point }=-69.55( \pm 5.17)+19.91( \pm 2.41) \chi \\
& \qquad r=0.992 \quad s=4.79^{\circ} \quad n=24 \quad 38.07( \pm 1.27) x^{v}
\end{aligned}
$$

Thus, $\delta^{v}$ values empirically derived from molar refraction are useful in correlating the boiling points in a mixed list of alkyl halides.

To test the consistency of the halogen parameters in a larger list with molecules containing oxygen and nitrogen, calculations of molar

Table VI—Boiling Points of Alkyl Halides

| Compound | Boiling Point |  | Residual | Connectivity Index |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Obs. | Calc. |  | $\chi^{c}$ | $\chi^{\nu}$ |
| Ethyl chloride | $13.0{ }^{\circ}$ | $17.9^{\circ}$ | -4.9 | 1.414 | 1.558 |
| Ethyl bromide | $38.0{ }^{\circ}$ | $38.9^{\circ}$ | -0.9 | 1.414 | 2.110 |
| Ethyl iodide | $72.0{ }^{\circ}$ | $77.8^{\circ}$ | -5.8 | 1.414 | 3.132 |
| Propyl chloride | $46.5{ }^{\circ}$ | $46.9^{\circ}$ | -0.4 | 1.914 | 2.058 |
| Propyl bromide | $71.0^{\circ}$ | $67.9^{\circ}$ | 3.1 | 1.914 | 2.610 |
| Propyl iodide | $102.5{ }^{\circ}$ | $106.8{ }^{\circ}$ | -4.3 | 1.914 | 3.632 |
| 1-Methylethyl chloride | $36.5{ }^{\circ}$ | $35.4{ }^{\circ}$ | 1.1 | 1.732 | 1.850 |
| 1-Methylethyl bromide | $60.0^{\circ}$ | $54.5^{\circ}$ | 7.5 | 1.732 | 2.300 |
| 1-Methylethyl iodide | $90.0{ }^{\circ}$ | $84.3{ }^{\circ}$ | 5.7 | 1.732 | 3.135 |
| 1-Methylpropyl chloride | $69.0{ }^{\circ}$ | $67.5^{\circ}$ | 1.5 | 2.270 | 2.414 |
| 1-Methylpropyl bromide | $91.0^{\circ}$ | $88.6{ }^{\circ}$ | 2.4 | 2.270 | 2.966 |
| 1-Methylpropyl iodide | $120.0^{\circ}$ | $127.5^{\circ}$ | -7.5 | 2.270 | 3.988 |
| 1,1-Dimethylethyl chloride | $51.0^{\circ}$ | $50.3^{\circ}$ | 0.7 | 2.000 | 2.102 |
| 1,1-Dimethylethyl bromide | $72.5{ }^{\circ}$ | $65.1^{\circ}$ | 7.4 | 2.000 | 2.492 |
| 1,1-Dimethylethyl iodide | $98.0{ }^{\circ}$ | $92.7^{\circ}$ | 5.3 | 2.000 | 3.215 |
| Butyl chloride | $78.0^{\circ}$ | $75.9^{\circ}$ | 2.1 | 2.414 | 2.558 |
| Butyl bromide | $101.0^{\circ}$ | $96.9^{\circ}$ | 4.1 | 2.414 | 3.110 |
| Butyl iodide | $130.0^{\circ}$ | $135.8^{\circ}$ | -5.8 | 2.414 | 4.132 |
| 1-Methylbutyl chloride | $97.0^{\circ}$ | $95.5^{\circ}$ | 1.5 | 2.770 | 2.888 |
| 1-Methylbutyl bromide | $117.0^{\circ}$ | $112.7^{\circ}$ | 4.3 | 2.770 | 3.338 |
| 1-Methylbutyl iodide | $142.0{ }^{\circ}$ | $144.5{ }^{\circ}$ | -2.5 | 2.770 | 4.173 |
| Propyl fluoride | $2.5{ }^{\circ}$ | $8.5{ }^{\circ}$ | -6.0 | 1.914 | 1.049 |
| Butyl fluoride | $32.5{ }^{\circ}$ | $37.5^{\circ}$ | -5.0 | 2.414 | 1.549 |
| Pentyl fluoride | $62.8{ }^{\circ}$ | $66.5^{\circ}$ | $-3.7$ | 2.914 | 2.049 |


| Compound | Molar Refraction |  | Connectivity Index |  | Compound | Molar Refraction |  | Connectivity Index |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Obs. | Calc. | $\chi^{c}$ | $\chi^{v}$ |  | Obs. | Calc. | $x^{c}$ | $\chi^{\nu}$ |
| Butyl methyl ether | 27.020 | 28.519 | 2.914 | 2.560 | 2-Ethyl-1-butanol | 31.180 | 32.163 | 3.346 | 2.955 |
| Dibutyl ether | 40.987 | 42.173 | 4.414 | 4.121 | 2-Methyl-2-pentanol | 31.210 | 30.225 | 3.060 | 2.784 |
| Dipropyl ether | 32.226 | 33.282 | 3.414 | 3.121 | 2-Methyl-3-pentanol | 31.138 | 31.068 | 3.180 | 2.861 |
| Ethyl 1-methylethyl ether | 27.678 | 27.695 | 2.770 | 2.504 | 4-Methyl-2-pentanol | 31.351 | 30.581 | 3.125 | 2.806 |
| Ethyl pentyl ether | 36.363 | 37.727 | 3.914 | 3.621 | 2,2-Dimethyl-1-butanol | 31.268 | 30.165 | 3.121 | 2.730 |
| 1-Methylpropyl ethyl ether | 31.560 | 32.478 | 3.308 | 3.042 | 3-Methyl-3-pentanol | 31.182 | 30.764 | 3.121 | 2.844 |
| Butyl 1-methylethyl ether | 36.027 | 36.586 | 3.770 | 3.504 | 2-Methyl-1-hexanol | 35.930 | 36.271 | 3.808 | 3.417 |
| 1-Methylpropyl methyl ether | 31.337 | 30.585 | 3.121 | 2.810 | 3-Ethyl-3-pentanol | 35.821 | 35.748 | 3.681 | 3.405 |
| Butyldimethylamine | 33.816 | 31.689 | 3.270 | 2.917 | 2-Ethyl-1-hexanol | 40.625 | 41.054 | 4.346 | 3.955 |
| Methyl-2-methylpropylamine | 33.852 | 34.520 | 4.201 | 2.806 | 2-Methyl-1-propanol | 22.103 | 22.597 | 2.270 | 1.879 |
| Dimethylpentylamine | 38.281 | 36.135 | 3.770 | 3.417 | 4-Ethyl-4-heptanol | 44.919 | 44.639 | 4.681 | 4.405 |
| Triethylamine | 33.793 | 32.764 | 3.346 | 3.070 | 6-Methyl-1-heptanol | 40.736 | 40.378 | 4.270 | 3.879 |
| Trimethylamine | 19.594 | 17.816 | 1.732 | 1.341 | 3-Methyl-3-heptanol | 40.446 | 39.655 | 4.121 | 3.844 |
| Tripropylamine | 47.783 | 46.100 | 4.846 | 4.570 | 4-Methyl-4-heptanol | 40.439 | 39.655 | 4.121 | 3.844 |
| 1-Aminopropane | 19.400 | 19.915 | 1.914 | 1.615 | 1-Octanol | 40.637 | 41.660 | 4.414 | 4.023 |
| 1-Aminobutane | 24.079 | 24.360 | 2.414 | 2.115 | 1-Chloropropane | 20.847 | 22.231 | 1.914 | 2.058 |
| 1-Amino-3-methylbutane | 28.672 | 27.523 | 2.770 | 2.471 | 2-Chlorobutane | 25.506 | 25.257 | 2.270 | 2.387 |
| 1-Aminopentane | 28.727 | 28.805 | 2.914 | 2.615 | 1-Chloro-2-methylpropane | 25.359 | 25.395 | 2.270 | 2.414 |
| 3-Aminopentane | 28.617 | 28.148 | 2.808 | 2.564 | 2-Chlorobutane | 25.440 | 26.677 | 2.414 | 2.558 |
| 1-Aminohexane | 33.290 | 33.251 | 3.414 | 3.115 | 3-Chloropentane | 30.160 | 30.040 | 2.808 | 2.925 |
| 1-Aminoheptane | 38.003 | 37.696 | 3.914 | 3.615 | 2-Bromopropane | 23.935 | 22.877 | 1.732 | 2.309 |
| 2-Aminoheptane | 38.037 | 36.701 | 3.770 | 3.526 | 1-Bromopropane | 23.679 | 25.176 | 1.914 | 2.621 |
| 1-Aminononane | 47.277 | 46.586 | 4.914 | 4.615 | 1-Bromo-2-methylpropane | 28.537 | 28.339 | 2.270 | 2.977 |
| 2-Propanol | 17.705 | 18.189 | 1.732 | 1.412 | 2-Bromobutane | 28.651 | 27.661 | 2.270 | 2.847 |
| 2-Pentanol | 26.680 | 27.418 | 2.770 | 2.450 | 1-Bromobutane | 28.347 | 29.621 | 2.414 | 3.121 |
| 3-Pentanol | 26.639 | 28.048 | 2.914 | 2.470 | 3-Bromopentane | 33.067 | 32.444 | 2.808 | 3.385 |
| 1-Hexanol | 31.428 | 32.769 | 3.414 | 3.023 | 2-Iodobutane | 33.939 | 32.297 | 2.270 | 3.733 |
| 1-Heptanol | 36.093 | 37.215 | 3.914 | 3.523 | 2-Iodopentane | 38.314 | 36.742 | 2.770 | 4.233 |
| 3-Methyl-1-butanol | 26.904 | 27.042 | 2.770 | 2.379 | 3-Iodopentane | 38.354 | 37.080 | 2.808 | 4.271 |
| 2-Methyl-1-butanol | 26.697 | 27.380 | 2.808 | 2.417 | 1-Iodopentane | 38.263 | 39.745 | 2.914 | 4.707 |
| 2-Methyl-2-butanol | 26.721 | 25.779 | 2.560 | 2.284 | 1-Iodohexane | 42.891 | 44.190 | 3.414 | 5.207 |
| 4-Methyl-1-pentanol | 31.489 | 31.487 | 3.270 | 2.879 | 1-Iodoheptane | 47.610 | 48.635 | 3.914 | 5.707 |
| 2-Methyl-i-pentanol | 31.164 | 31.825 | 3.308 | 2.917 |  |  |  |  |  |

refraction were compared with experimentally derived values (Table VII). The consistency of all $\delta^{v}$ values appears to be quite good as seen from:

$$
\begin{gather*}
R_{m}=4.460+5.230( \pm 0.211) \chi^{\nu}+3.661( \pm 0.227) \chi \\
r=0.990 \quad s=1.022 \quad n=65 \tag{Eq.13}
\end{gather*}
$$

## CONCLUSIONS

A set of valence $\delta$ values were developed for use in calculating the connectivity index, $\chi$, for heteroatom-containing molecules. The improvement in the correlations with the boiling point and molar refraction for a wide range of molecules suggests the general applicability of these values.

The use of the number of valence electrons together with the number of attached hydrogen atoms provides a firm relationship between the structural characteristics expressed in the hydrogensuppressed graph and the properties of molecules (3).

An important advance is made by this development in that drug molecules containing heteroatoms may now be considered with a more sophisticated molecular connectivity treatment. These $\delta^{v}$ values are currently being used in biological studies in this laboratory (3, 9).

## REFERENCES

(1) L. B. Kier, L. H. Hall, W. J. Murray, and M. Randić, J. Pharm. Sci., 64, 1971(1975).
(2) L. H. Hall, L. B. Kier, and W. J. Murray, ibid., 64,

1974(1975)
(3) L. B. Kier and L. H. Hall, '"Molecular Connectivity in Chemistry and Drug Research," Academic, New York, N.Y., 1976.
(4) W. J. Murray, L. B. Kier, and L. H. Hall, J. Pharm. Sci., 64, 1978(1975).
(5) L. B. Kier, W. J. Murray, and L. H. Hall, J. Med. Chem., 18, 1272(1975).
(6) W. J. Murray, L. B. Kier, and L. H. Hall, ibid., 19, 573(1976).
(7) L. B. Kier, W. J. Murray, M. Randic, and L. H. Hall, J. Pharm. Sci., 65, 1226(1976).
(8) F. E. Norrington, R. M. Hyde, S. G. Williams, and R. Wooten, J. Med. Chem., 18, 604(1975).
(9) L. H. Hall and L. B. Kier, J. Pharm. Sci., in press.

## ACKNOWLEDGMENTS AND ADDRESSES

Received October 9, 1975, from the *Massachusetts College of Pharmacy, Boston, MA 02115, and the ${ }^{\ddagger}$ Eastern Nazarene College, Quincy, MA 02170

Accepted for publication February 23, 1976.
Supported in part by a grant from the Research Corp. and by Grant DA01353 from the National Institutes of Health.

The authors thank Mr. Phillip Coy for assistance with computerized calculations and the computer centers at Eastern Nazarene College and Massachusetts College of Pharmacy for use of their facilities.
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[^0]:    a Boiling points were taken from the "Handbook of Tables for Organic Compound Identification," 3rd ed., CRC Press, Cleveland, Ohio, 1967.

